

# Reasoning and Problem Solving

## Step 10: Add Fractions

### National Curriculum Objectives:

Mathematics Year 5: (5F2a) [Recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements  \$> 1\$  as a mixed number \[for example,  \$2/5 + 4/5 = 6/5 = 1 \frac{1}{5}\$ \]](#)

Mathematics Year 5: (5F4) [Add and subtract fractions with the same denominator and denominators that are multiples of the same number](#)

### Differentiation:

Questions 1, 4 and 7 (Reasoning)

**Developing** Explain whether a calculation of 3 fractions is true or false. Denominators are the same or halves or doubles of each other.

**Expected** Explain whether a calculation of 3 fractions is true or false. Denominators are multiples of the same number.

**Greater Depth** Explain whether a calculation of 3 fractions is true or false. Denominators are not multiples of the same number but have common factors.

Questions 2, 5 and 8 (Problem Solving)

**Developing** Find more than one combination of 3 fractions, from a choice of 4, whose sum is below a given limit ( $> 1$ ). Denominators are the same or halves or doubles of each other.

**Expected** Find more than one combination of 3 fractions, from a choice of 4, whose sum is below a given limit ( $> 1$ ). Denominators are multiples of the same number.

**Greater Depth** Find more than one combination of 3 fractions, from a choice of 4, with a sum falling within a given range ( $> 1$ ). Denominators are not multiples of the same number but have common factors.

Questions 3, 6 and 9 (Problem Solving)

**Developing** Find 3 possible solutions to a fraction riddle by adding fractions whose denominators are the same or halves or doubles of each other.

**Expected** Find 3 possible solutions to a fraction riddle when adding fractions. Denominators are multiples of the same number.

**Greater Depth** Find 3 possible solutions to a fraction riddle when adding fractions. Denominators are not multiples of the same number but have common factors.

More [Year 5 Fractions](#) resources.

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## Add Fractions

1a. True or false? Explain your answer.

$$\frac{2}{3} + \frac{1}{3} + \frac{5}{6} = 1 \frac{8}{12}$$



R

## Add Fractions

1b. True or false? Explain your answer.

$$\frac{3}{5} + \frac{4}{5} + \frac{9}{10} = 2 \frac{5}{10}$$



R

2a. Select 3 fractions which add up to no more than  $1 \frac{5}{8}$ .

$\frac{3}{8}$	$\frac{5}{8}$	$\frac{1}{4}$	$\frac{3}{4}$
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Find more than one answer.



PS

2b. Select 3 fractions which add up to no more than  $1 \frac{4}{6}$ .

$\frac{1}{6}$	$\frac{2}{3}$	$\frac{5}{6}$	$\frac{1}{3}$
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Find more than one answer.



PS

3a. Find 3 possible solutions to the riddle.

I have 3 proper fractions, their sum is greater than  $1 \frac{1}{8}$ .

Each denominator is the same even single digit below 5.

What could my fractions be?



PS

3b. Find 3 possible solutions to the riddle.

I have 3 proper fractions, their sum is between  $1 \frac{1}{3}$  and  $2 \frac{1}{3}$ .

Each denominator is a multiple of 3, and less than 7. All numerators are the same single digit.

What could my fractions be?



PS

## Add Fractions

4a. True or false? Explain your answer.

$$\frac{3}{4} + \frac{11}{12} + \frac{7}{24} = 1 \frac{21}{24}$$



R

## Add Fractions

4b. True or false? Explain your answer.

$$\frac{3}{9} + \frac{2}{3} + \frac{10}{15} = \frac{25}{15}$$



R

5a. Select 3 fractions which add up to no more than  $1 \frac{1}{2}$ .

$\frac{2}{6}$	$\frac{2}{3}$	$\frac{13}{24}$	$\frac{5}{12}$
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Find more than one answer.



PS

5b. Select 3 fractions which add up to no more than  $1 \frac{9}{10}$ .

$\frac{2}{5}$	$\frac{7}{10}$	$\frac{9}{20}$	$\frac{7}{15}$
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Find more than one answer.



PS

6a. Find 3 possible solutions to the riddle.

I have 3 proper fractions, their sum is  $\frac{1}{4}$  greater than  $1 \frac{5}{8}$ .

Each denominator is a different, single digit and a multiple of 2.

What could my fractions be?



PS

6b. Find 3 possible solutions to the riddle.

I have 3 proper fractions, their sum is between 1 and  $1 \frac{2}{3}$ .

Each denominator is a different, single digit and a multiple of 3.

What could my fractions be?



PS

## Add Fractions

7a. True or false? Explain your answer.

$$\frac{2}{5} + \frac{2}{3} + \frac{5}{6} = 1 \frac{3}{10}$$



R

## Add Fractions

7b. True or false? Explain your answer.

$$\frac{3}{12} + \frac{7}{9} + \frac{1}{4} = 1 \frac{5}{18}$$



R

8a. Select 3 fractions to make a total between  $1 \frac{3}{4}$  and  $1 \frac{11}{12}$ .

$\frac{5}{8}$	$\frac{2}{3}$	$\frac{3}{6}$	$\frac{7}{12}$
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Find more than one answer.



PS

8b. Select 3 fractions to make a total between  $1 \frac{1}{2}$  and 2.

$\frac{7}{10}$	$\frac{1}{5}$	$\frac{5}{8}$	$\frac{3}{4}$
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Find more than one answer.



PS

9a. Find 3 possible solutions to the riddle.

I have 3 proper fractions, their sum is  $\frac{1}{28}$  greater than  $1 \frac{3}{7}$ .

Each denominator is a different factor of 28.

What could my fractions be?



PS

9b. Find 3 possible solutions to the riddle.

I have 3 proper fractions, their sum is between  $1 \frac{2}{5}$  and  $1 \frac{9}{10}$ .

Each denominator is a different factor of 20.

What could my fractions be?



PS

**Developing**

1a. False; the numerators and denominators have been added without finding common denominator.

$$\frac{2}{3} + \frac{1}{3} + \frac{5}{6} = 1 \frac{5}{6}$$

2a. Various possible answers, for example:

$$\frac{3}{8} + \frac{5}{8} + \frac{1}{4} \text{ or } \frac{3}{8} + \frac{1}{4} + \frac{3}{4}$$

3a. Various possible answers, for example:

$$\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \text{ or } \frac{1}{4} + \frac{1}{4} + \frac{3}{4} \text{ or } \frac{1}{4} + \frac{2}{4} + \frac{3}{4}$$

**Expected**

4a. False; the numerators have been added without finding a common denominator.

$$\frac{3}{4} + \frac{11}{12} + \frac{7}{24} = 1 \frac{23}{24}$$

5a. 2 possible answers:

$$\frac{2}{6} + \frac{2}{3} + \frac{5}{12} \text{ or } \frac{2}{6} + \frac{13}{24} + \frac{5}{12}$$

6a. Various possible answers, for example:

$$\frac{1}{2} + \frac{3}{4} + \frac{5}{8} \text{ or } \frac{3}{6} + \frac{3}{4} + \frac{5}{8} \text{ or } \frac{1}{2} + \frac{2}{4} + \frac{7}{8}$$

**Greater Depth**

7a. False; the solution has been incorrectly simplified.

$$\frac{2}{5} + \frac{2}{3} + \frac{5}{6} = 1 \frac{9}{10}$$

8a. Various possible answers, for example:

$$\frac{5}{8} + \frac{2}{3} + \frac{3}{6} \text{ or } \frac{5}{8} + \frac{2}{3} + \frac{7}{12}$$

9a. Various possible answers, for example:

$$\frac{1}{2} + \frac{3}{4} + \frac{3}{14} \text{ or } \frac{1}{2} + \frac{1}{4} + \frac{10}{14} \text{ or } \frac{1}{2} + \frac{1}{4} + \frac{5}{7}$$

**Developing**

1b. False; they the tenths have also been doubled rather than just the fifths.

$$\frac{3}{5} + \frac{4}{5} + \frac{9}{10} = 2 \frac{3}{10}$$

2b. Various possible answers, for example:

$$\frac{1}{6} + \frac{2}{3} + \frac{1}{3} \text{ or } \frac{5}{6} + \frac{1}{6} + \frac{1}{3}$$

3b. Various possible answers, for example:

$$\frac{2}{3} + \frac{2}{3} + \frac{2}{3} \text{ or } \frac{2}{3} + \frac{2}{3} + \frac{2}{6} \text{ or } \frac{3}{6} + \frac{3}{6} + \frac{3}{6}$$

**Expected**

4b. True; the calculation is correct and presented as an improper fraction. It could also be written as a mixed number and simplified.

$$\frac{3}{9} + \frac{2}{3} + \frac{10}{15} = \frac{25}{15} = 1 \frac{2}{3}$$

5b. Various possible answers, for example:

$$\frac{2}{5} + \frac{7}{10} + \frac{9}{20} \text{ or } \frac{2}{5} + \frac{7}{10} + \frac{7}{15}$$

6b. Various possible answers, for example:

$$\frac{1}{3} + \frac{4}{6} + \frac{3}{9} \text{ or } \frac{1}{3} + \frac{2}{6} + \frac{6}{9} \text{ or } \frac{2}{3} + \frac{2}{6} + \frac{3}{9}$$

**Greater Depth**

7b. True; the calculation is correct and presented in its simplest form.

$$\frac{3}{12} + \frac{7}{9} + \frac{1}{4} = \frac{46}{36} = 1 \frac{10}{36} = 1 \frac{5}{18}$$

8b. 2 possible answers:

$$\frac{7}{10} + \frac{1}{5} + \frac{3}{4} \text{ or } \frac{1}{5} + \frac{5}{8} + \frac{3}{4}$$

9b. Various possible answers, for example:

$$\frac{1}{2} + \frac{2}{4} + \frac{3}{5} \text{ or } \frac{1}{2} + \frac{1}{5} + \frac{9}{10} \text{ or } \frac{2}{4} + \frac{2}{5} + \frac{7}{10}$$